## ETT\_2026 Digitaalinen Signaalinkäsittely Exam

## May 09, 2018

Students are allowed to use only calculator. The necessary equations and references are given in the last two pages of this exam paper.

- 1. Describe the following. (5 p)
  - a) Linear time-invariant system and its properties.
  - b) Specify some of the basic purposes of filters and give type of applications where the filters are needed.
  - c) Give list of applications where adaptive signal processing is used and what are its benefits compared to non-adaptive signal processing?
  - d) Define multirate signal processing and why it is needed?
  - e) Describe the purpose of FFT and its applications?
- 2. The impulse response of a system is given as follows h(n) = {0.5, -3, -2, 1, 0, 4} (4 pt)
  - a) Determine the corresponding frequency response at frequency  $\omega = 0.5^{*}2\pi$ .
  - b) What is the system response if the system input is  $x(z) = 1/1-z^{-1}$
- 3. Design a lowpass FIR filter that satisfy the specifications:  $\omega_p = 0.3\pi$ ,  $A_p = 0.5 dB$ ,  $\omega_s = 0.5\pi$ , and  $A_s = 50 dB$ . (8 pt)
  - a) Use an appropriate fixed window to obtain a minimum order linear-phase filter and determine the coefficients of the impulse response of the filter and plot it.
  - b) What will be the order of the filter if it uses Kaiser window?
- 4. The system function of a discrete-time LTI system is as follows (8 pt)

$$H(z) = \frac{z^2 + 0.3z + 1}{z^2 + 0.2z + 1.4}$$

- a) Determine the time-domain difference equation of the system.
- b) Draw direct form II structure of the system.
- c) Calculate the output of the system when the input is  $x(n) = 3 + sin(0.5\pi n)$
- d) Is the system stable, why?